

Homework 1  
Due January 22, 2008



1. You are given two intersecting straight lines and a point  $P$  marked on one of them. Show how to construct, using a straightedge and compass, a circle that is tangent to both lines and that has the point  $P$  as its point of tangency to one of the lines.

2. Determine a simple formula for the series  $\sum_{k=1}^n \frac{k}{(k+1)!}$ .

3. Let  $P(x)$  and  $Q(x)$  be polynomials whose coefficients are the same but in "backwards order":

$$P(x) = a_0 + a_1x + a_2x^2 + \cdots + a_nx^n$$

$$Q(x) = a_n + a_{n-1}x + a_{n-2}x^2 + \cdots + a_0x^n$$

What is the relationship between the roots of  $P(x)$  and  $Q(x)$ ? Prove your answer.

4. Consider the parallelogram  $ABCD$  with diagonals  $AC$  and  $BD$ . State all the properties of the figure that you are willing to accept. Then give a complete argument justifying why you believe your assertions to be correct.